A factor of integer polynomials with minimal integrals

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We give a quick description of an elementary and clever method of Gelfond, Shnirelman, and Nair to prove lower bound for the Chebyshev's function $\psi(x)$. This method leads to the study of the set S_N of polynomials with integer coefficients, degree less than N, and minimal nonzero integral over $[0, 1]$.

In particular, Bazzanella proved some results about the factors of the polynomials in S_N. We illustrate an improvement of these results and we raise some open questions.

Riferimenti bibliografici

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